

Modeling Cyclical Growth

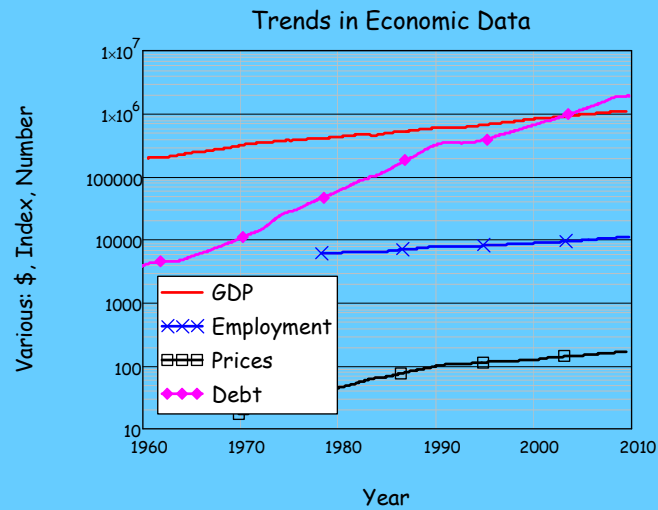
Steve Keen
School of Economics & Finance
University of Western Sydney

The Project

- UNEP specification of non-equilibrium economic model
 - Linked to CSIRO bio-physical model
- My brief:
 - Take single sectoral model of cycles (Keen 1995 etc.)
 - Single sectoral model of credit (Keen 2009 etc.)
 - Combine into multi-sectoral cyclical model of credit and production
 - ***Never previously done***
 - Previous attempts at dynamic "IO" input-output (multi-sectoral) models generally failed
 - Fatal instabilities—negative prices etc.
 - No previous attempts to model multisectoral ***monetary*** dynamics

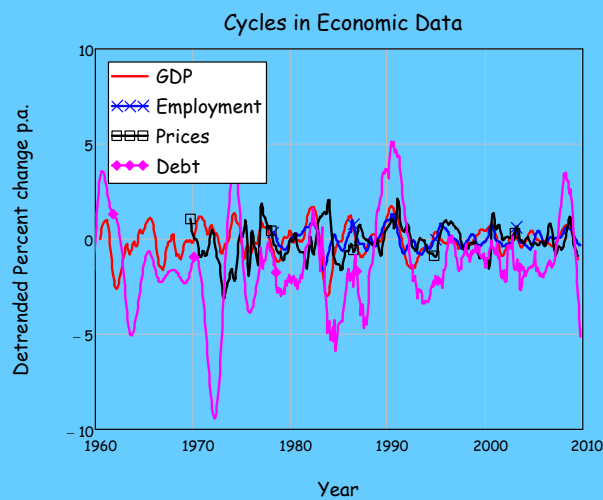
Trends in economic data

- Growth the norm in market economies...



Cycles in economic data

- As are cycles...
 - Previous data, de-trended:



Conventional economic models

- "Neoclassical" General Equilibrium models
 - Focus on trend
 - Ignore cycles
 - Ignore money
 - Presume system is
 - In equilibrium unless "shocked"
 - Will return to equilibrium after "exogenous shock"
 - Yet models have "dual instability" dilemma
 - Prices or quantities or both *must* be unstable
 - Effectively a barter system
 - Money only affects relative prices & inflation
- Cycles assumed to be caused by *noneconomic* factors
 - Agriculture/weather/sunspots... (meteors?)

Conventional economic models

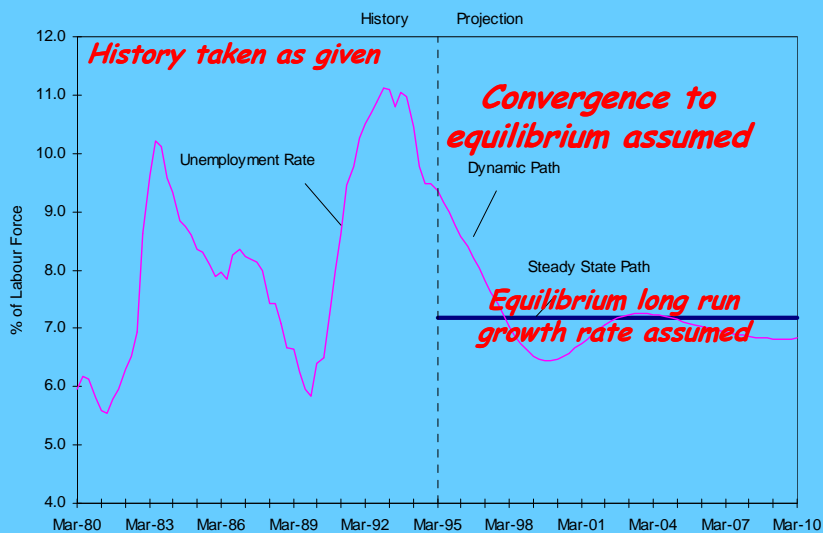
- "The capitalistic economy is stable, and absent some change in technology or the rules of the economic game, the economy converges to a constant growth path with the standard of living doubling every 40 years."
 - Edward C. Prescott (Nobel Prize 2004 for Real Business Cycle Theory), [1999](#)
- "As ... discussed in ... "The Dynamic General Equilibrium Model," the model features a representative household [*i.e.*, *one only!*] that chooses paths of consumption, leisure, and investment to maximize utility. *The paths of TFP and population are exogenously given, and the agent has perfect foresight over their values. We start the model at date $T_0 = 1980$ and let time run out to infinity...*"
Conesa [2007](#)

Conventional economic models

- "The model could be described as broadly new Keynesian in its dynamic structure **but with an equilibrating long run.**
- Activity is demand determined in the short run but supply determined in the long run...
- **The model will eventually return to a supply determined equilibrium growth path in the absence of demand or other shocks."**
 - Australian Treasury TRYM Model ([2001](#))
- Cycles treated as exogenous to model of economy...

Conventional economic models

- E.g. unemployment in Australian Treasury TYRM model



Conventional economic models

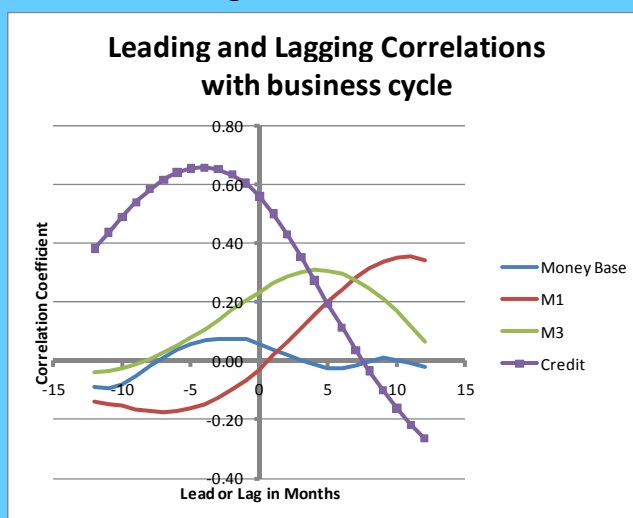
- Treatment of money and debt
 - In general, money ignored
 - "One thing which has not changed over the past five years is the philosophy underpinning the model.
 - It remains small, highly aggregated, empirically based, **and non-monetary in nature.**" Australia's RBA ([2005](#))
 - Money "neutrality" assumed
 - Affects price level but not real output
 - Universally, private debt ignored
- Versus empirical data...

Endogenous Money

- "The fact that the transaction component of real cash balances (M_1) moves contemporaneously with the cycle
- while the much larger nontransaction component (M_2) leads the cycle
- suggests that credit arrangements could play a significant role in future business cycle theory.
- *Introducing money and credit into growth theory in a way that accounts for the cyclical behavior of monetary as well as real aggregates is an important open problem in economics.*
 - Kydland and Prescott ([1990](#), p. 15. Emphasis added)
- 1990 analysis confirmed by more recent data
 - E.g., leads and lags for Australia 1954-2009:

Endogenous Money

- Credit leads cycle with significant correlation
- All other variables lag or have low correlations:



Key role of private debt

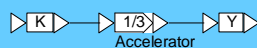
- "Our tests produce a clear story about short-term financing decisions in response to earnings and investment...
 - The leverage and debt regressions then confirm that, for dividend payers, *debt is indeed the residual variable in financing decisions.*
 - Like dividend payers, non-payers primarily *use debt to absorb short-term variation in earnings and investment.*" (Fama & French [2000](#); emphases added)

Objectives for our economic model

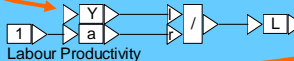
- Non-equilibrium
 - Economy itself inherently & endogenously cyclical
 - Model had to represent this
- Multi-sectoral
 - Many non-neoclassical endogenous cycle models
 - But none to date were multi-sectoral
- Explicitly monetary
 - Key role of money & debt shown in data
 - Incorporate interplay of debt, money and cycles
- 3 key foundations
 - Goodwin "Growth Cycle" model (1967)
 - Minsky "Financial Instability Hypothesis"
 - Graziani "Circuit Theory" model of credit creation

Foundations (1) Cycles: Goodwin's "Growth Cycle"

- Capital K determines output Y via the accelerator:



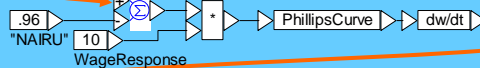
- Y determines employment L via productivity a :



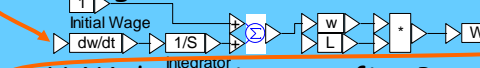
- L determines employment rate l via population N :



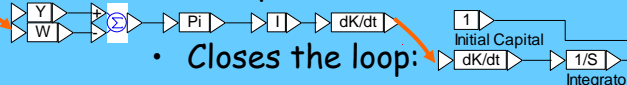
- l determines rate of change of wages w via P.C.



- Integral of w determines W (given initial value)



- $Y-W$ determines profits P and thus Investment I ...

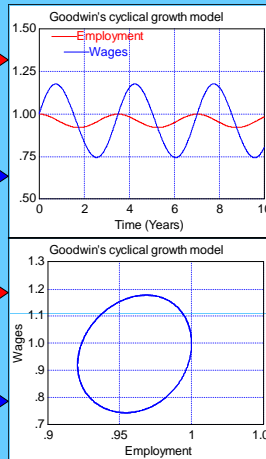
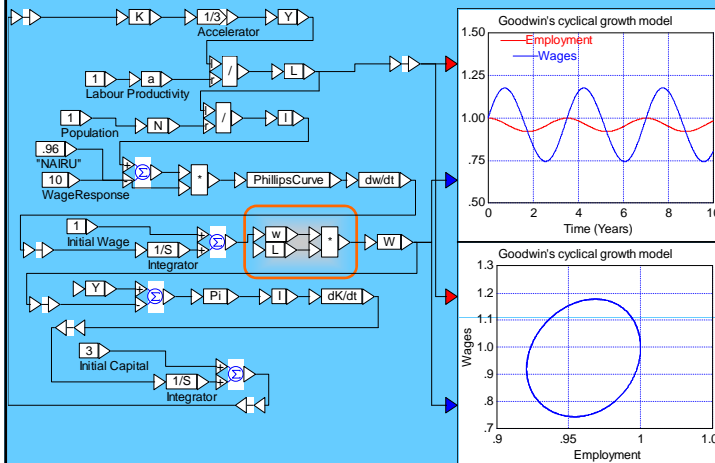


- Closes the loop:

Foundations (1) Cycles: Goodwin's "Growth Cycle"

- Goodwin's "Lokta-Volterra" model generates cycles: 

Goodwin01B.vsm



- Cycles caused by **essential** nonlinearity:
- Wage rate times employment
- Behavioural nonlinearities not needed for cycles;
- Instead, restrain values to realistic levels

Foundations (2) Debt: Minsky's "FIH"

- Only theory that predicts this financial crises:
 - "it is necessary to have an economic theory which makes great depressions one of the possible states in which our type of capitalist economy can find itself."
(*Can "It" Happen Again? A Reprise*)
- Time-&-debt-aware model:
 - Economy in historical time
 - Debt-induced recession in recent past
 - Firms and banks conservative re debt/equity, assets
 - Only conservative projects are funded
 - Recovery means most projects succeed
 - Firms and banks revise risk premiums
 - Accepted debt/equity ratio rises
 - Assets revalued upwards...

Foundations (2) Debt: Minsky's "FIH"

- Period of tranquility causes expectations to rise...
 - "Stability—or tranquility—in a world with a cyclical past and capitalist financial institutions is destabilizing." (*The Financial Instability Hypothesis: A Restatement*)
- Self-fulfilling expectations
 - Decline in risk aversion causes increase in investment
 - Investment expansion causes economy to grow faster
 - Asset prices rise
 - speculation on assets profitable
 - Increased willingness to lend increases money supply
 - Money supply endogenous money, not under Fed control
 - Riskier investments enabled, asset speculation rises
- The emergence of "Ponzi" financiers
 - Cash flow less than debt servicing costs
 - Profit by selling assets on rising market
 - Interest-rate insensitive demand for finance

Foundations (2) Debt: Minsky's "FIH"

- Eventually:
 - Rising rates make conservative projects speculative
 - Non-Ponzi investors sell assets to service debts
 - Entry of new sellers floods asset markets
 - Rising trend of asset prices falters or reverses
- Ponzi financiers go bankrupt:
 - Can no longer sell assets for a profit
 - Debt servicing on assets far exceeds cash flows
- Asset prices collapse, increasing debt/equity ratios
- Endogenous expansion of money supply reverses
- Investment evaporates; economic growth slows
- Economy enters a debt-induced recession
 - Back where we started...

Foundations (3): Endogenous money

- Fundamental Endogenous Money insight
 - "Loans create Deposits"
 - Reverse of "Money Multiplier" model
- Suggested directly modeling bank credit creation via account dynamics
 - Simple model of "Wicksellian" pure credit economy
 - No government sector or fiat money (yet)
 - Explicitly monetary model
 - "Double-entry book-keeping" meets symbolic math

Foundations (3): Endogenous money

- New methodology for dynamic modelling
 - Table where each column represents a stock
 - Each row represents relations between system states...

Dynamic System					
	"System States"				
	Stock A	Stock B	...	Stock Z	Accounting
	Flow 1	- Flow 1	...		Sum(=0)
Flows	+ Flow 2	- Flow 2	Sum

$\frac{d}{dt} A(t)$ $\frac{d}{dt} B(t)$ $\frac{d}{dt} Z(t)$

- To generate the model, symbolically add up each column
 - Sum of column is differential equation for stock
 - Continuous time, not "discrete" time
 - *Strictly* monetary model of *pure credit* multi-commodity production economy developed...

Foundations (3): Endogenous money

- Input system as table:

"Type"	0	1	-1	-1	0
"Account"	"Bank Reserves"	"Firm Loan"	"Firm Deposit"	"Worker Deposit"	"Bank Income"
"Account"	$B_R(t)$	$F_L(t)$	$F_D(t)$	$W_D(t)$	$B_I(t)$

$S_2 :=$

- Interest flows: bank \leftrightarrow firm
- Wage flows: firm \rightarrow workers
- Interest flows: bank \rightarrow workers
- Consumption flows: bank & workers \rightarrow firms
- Debt repayment flows: firms \rightarrow bank
- Reserve relending flows: bank \rightarrow firms
- New Money/Debt flows: bank \leftrightarrow firms

- Symbolic substitutions for placeholders above:
- E.g., A is "loan interest rate times outstanding debt"

$$A = r_L \cdot F_L(t)$$
- Time lags used for behavioural variables

Foundations (3): Endogenous money

- Simple code develops mode automatically:

Over to Mathcad...

```

SystemODEs(x) :=
  Functions ← submatrix(x, 2, 2, 1, cols(x) - 1)
  Equations ← submatrix(x, 3, rows(x) - 1, 1, cols(x) - 1)
  for i ∈ 0..cols(Functions) - 1
    E_i ← d/dt Functions_i = ∑ Equations_i
  return E
  
```

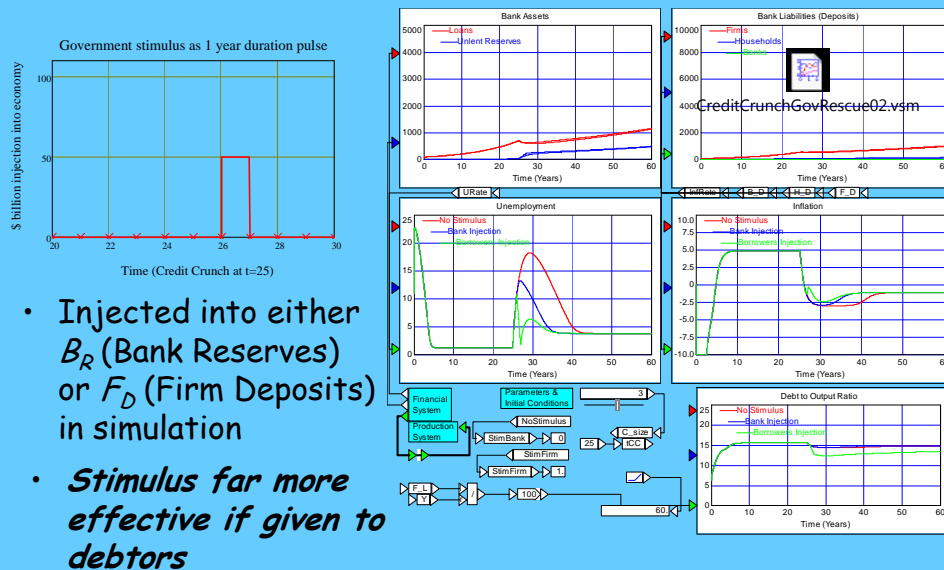
$$\text{SystemODEs}(S_2) \rightarrow \left[\begin{array}{l}
 \frac{d}{dt} B_R(t) = \frac{F_L(t)}{\tau_L} - \frac{B_R(t)}{\tau_R} \\
 \frac{d}{dt} F_L(t) = \frac{B_R(t)}{\tau_R} + \frac{F_D(t)}{\tau_M} - \frac{F_L(t)}{\tau_L} \\
 \frac{d}{dt} F_D(t) = r_D \cdot F_D(t) - r_L \cdot F_L(t) + \frac{B_I(t)}{\tau_B} + \frac{B_R(t)}{\tau_R} + \frac{F_D(t)}{\tau_M} - \frac{F_L(t)}{\tau_L} + \frac{W_D(t)}{\tau_W} + \frac{F_D(t) \cdot (s-1)}{\tau_S} \\
 \frac{d}{dt} W_D(t) = r_D \cdot W_D(t) - \frac{W_D(t)}{\tau_W} - \frac{F_D(t) \cdot (s-1)}{\tau_S} \\
 \frac{d}{dt} B_I(t) = r_L \cdot F_L(t) - r_D \cdot F_D(t) - r_D \cdot W_D(t) - \frac{B_I(t)}{\tau_B}
 \end{array} \right]$$

Modelling a Credit Crunch

- Simple production model linked to financial flows
 - Output is Labour times productivity $Q = a \cdot L$
 - Labour is Money Wages flow divided by Money Wage rate $L = \frac{1-s}{\tau_s} \cdot \frac{F_D}{W}$
 - Wage set by Phillips curve unemployment-money wage change function $\frac{1}{W} \cdot \frac{dW}{dt} = \rho_h \left(\frac{L}{N} \right)$
 - Price (necessary link between \$ accounts and physical output) lagged convergence to markup over monetary cost of production $\frac{d\rho}{dt} = -\frac{1}{\tau_p} \cdot \left(\rho - \frac{W}{a \cdot (1-s)} \right)$
- Single sectoral model generates stable dynamics
- Can be used to consider some policy questions
 - But no cycles as yet
- Policy example—stimulus to overcome credit crunch

Modelling a Credit Crunch

- What's better? Stimulus to lenders or debtors?



- Injected into either B_R (Bank Reserves) or F_D (Firm Deposits) in simulation
- *Stimulus far more effective if given to debtors*

Producing a multi-sectoral nonequilibrium model

- Minsky model
 - Goodwin cycles
 - Debt "ratchets up" of in series of cycles
 - With "Ponzi lending", tends towards Depression
 - But implicit money only (debt to GDP ratio)
- Graziani model
 - Explicit money
 - Monetary determination of equilibrium output
 - But no cycles
- Blending two models *necessitates* multi-sectoral model
 - Capital sector for purchases of investment goods
 - Easily built using "Table to Dynamic Model" technology

A Multi-sectoral monetary model

- More complicated table (2 sector version shown here):

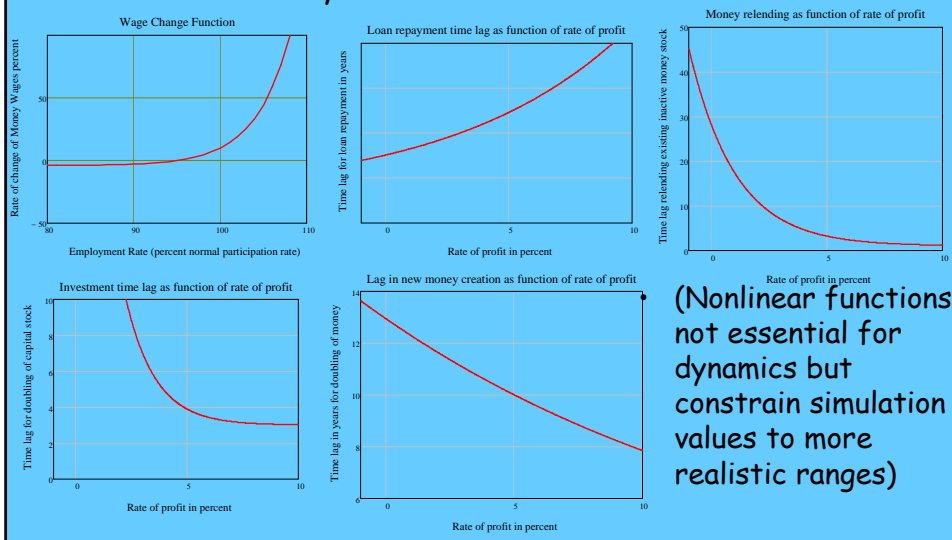
"Type"	0	1	1	1	1	-1	-1	-1	-1	-1	0
"Name"	"BR"	"K1 L"	"K2 L"	"C1 L"	"C2 L"	"K1 D"	"K2 D"	"C1 D"	"C2 D"	"W D"	"B F"
"Symbol"	$B_p(t)$	$F_{LK}(t)$	$F_{LK}(t)$	$F_{LC}(t)$	$F_{LC}(t)$	$F_{DK}(t)$	$F_{DK}(t)$	$F_{DC}(t)$	$F_{DC}(t)$	$W_y(t)$	$B_f(t)$
"Compounding Debt"	0	A	B	C	D	0	0	0	0	0	0
"Deposit Interest"	0	0	0	0	0	E	F	G	H	0	-(E + F + G + H)
"Investment"	0	0	0	0	0	-1 + (I + K)	-1 + (I + L)	-K	-L	0	0
"Wages"	0	0	0	0	0	-M	-N	-O	-P	M + N + O + P	0
"Intersectoral Demand"	0	0	0	0	0	-Q	-R	-S + (Q + T)	-T + (R + S)	0	0
"Interest Workers"	0	0	0	0	0	0	0	0	0	U	-U
"Pay Interest"	0	-V	-W	-X	-Y	-V	-W	-X	-Y	0	V + W + X + Y
"Consumption"	0	0	0	0	0	-Z	-AA	$-AB + \left(Z + AC + \frac{AD + AE}{2} \right)$	$-AC + \left(AA + AB + \frac{AD + AE}{2} \right)$	-AD	-AE
"Repay Loans"	AF + AG + AH + AI	-AF	-AG	-AH	-AI	-AF	-AG	-AH	-AI	0	0
"Recycle Reserves"	-(AJ + AK + AL + AM)	AJ	AK	AL	AM	AJ	AK	AL	AM	0	0
"New Money"	0	AN	AO	AP	AQ	AN	AO	AP	AQ	0	0

- Capital and Consumer Goods Sectors
 - All sectors in 2 halves to force recording of intra-sectoral monetary purchases
- Investment & inter-sectoral demand
- Time lags are time-varying functions of rate of profit rather than constant parameters

$$\begin{pmatrix} 1 \\ J \\ K \\ L \end{pmatrix} = F_{\text{Deposits}} + \begin{pmatrix} \tau_{pr}(pr_K(t)) \\ \tau_{pr}(pr_K(t)) \\ \tau_{pr}(pr_C(t)) \\ \tau_{pr}(pr_C(t)) \end{pmatrix} \rightarrow \begin{pmatrix} F_{DK1}(t) \\ \tau_{pr}(pr_K(t)) \\ F_{DK2}(t) \\ \tau_{pr}(pr_K(t)) \\ F_{DC1}(t) \\ \tau_{pr}(pr_C(t)) \\ F_{DC2}(t) \\ \tau_{pr}(pr_C(t)) \end{pmatrix}$$

A Multi-sectoral monetary model

- More complex financial model results
 - Constrained by nonlinear behavioural relations



(Nonlinear functions not essential for dynamics but constrain simulation values to more realistic ranges)

A Multi-sectoral monetary model

- Allied to lagged Goodwin growth cycle production model
 - Investment minus Depreciation determines Capital

$$\frac{d}{dt} K_{K1}(t) = \frac{F_{DK1}(t)}{\tau_{pr}(pr_K(t)) \cdot P_{K1}(t)} - \gamma \cdot K_{K1}(t)$$

- Output function of capital stock $\frac{d}{dt} Q_{K1}(t) = \frac{-1}{\tau_{QK}} \left[Q_{K1}(t) - \frac{1}{v_K} (K_{K1}(t)) \right]$

- Employment function of output $\frac{d}{dt} L_{K1}(t) = \frac{-1}{\tau_{LK}} \left(L_{K1}(t) - \frac{Q_{K1}(t)}{a_K(t)} \right)$

- Model of financially driven cyclical economy
 - Simulations shown here lead to sustained cycles
 - (No speculative debt in model as yet)
- Overall system very complex
 - But easily simulated in modern software
 - Scales indefinitely (more sectors easily added)

A Multi-sectoral monetary model

- Model requires minimum of

- $4n+3$ financial ODEs
- $2n$ Loan & $2n$ Deposit
- Bank Income
- Bank Reserves
- Household Deposit

- $5n$ sectoral equations

- capital, output, labour, prices, productivity

- 1 population equation

- 40 ODEs in this 4 sector model



A Multi-sectoral monetary model

- Notional Sectors in system shown here:

- Capital Goods
- Consumer Goods
- Agriculture
- Energy

- Generates complex endogenous cycles in income shares, output, credit, employment—just like actual economy

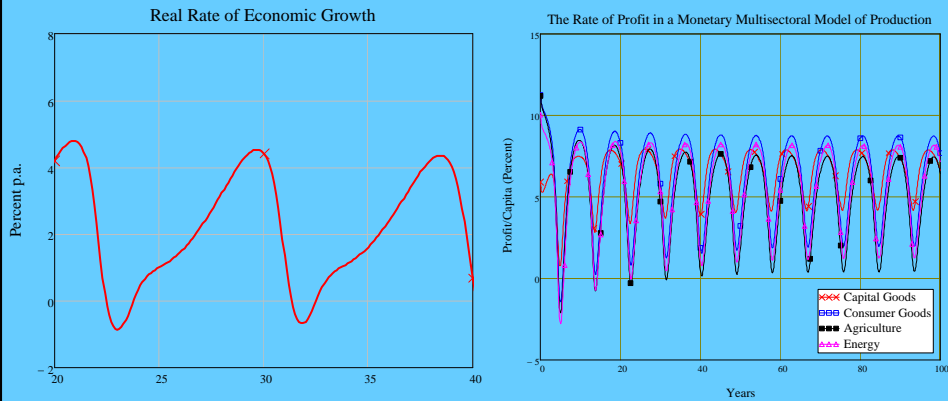
- No need for "exogenous shocks"
 - Though can also be added in future

- Not yet fitted to empirical data

- But *qualitative* behaviour of model matches "stylised facts" of (credit-driven) business cycle

A Multi-sectoral monetary model of production

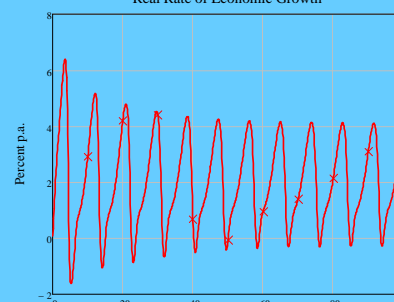
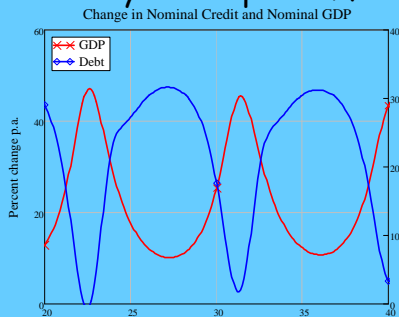
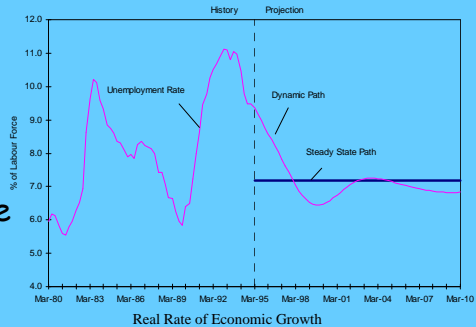
- Endogenous cycles...



- Cycles similar to stylised facts of business cycle
 - Long accelerating boom
 - Sudden slump
 - Tepid recovery before next boom

A Multi-sectoral monetary model of production

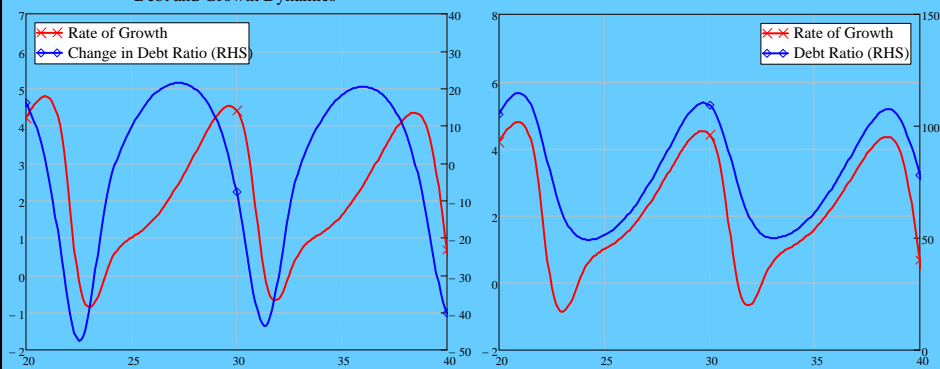
- With equilibrium models
 - History cyclical
 - The future equilibrium...
- With non-equilibrium model, projections look like history
 - Cycles in past & future



A Multi-sectoral monetary model of production

- Crucial role of credit
 - Change in credit leads cycle

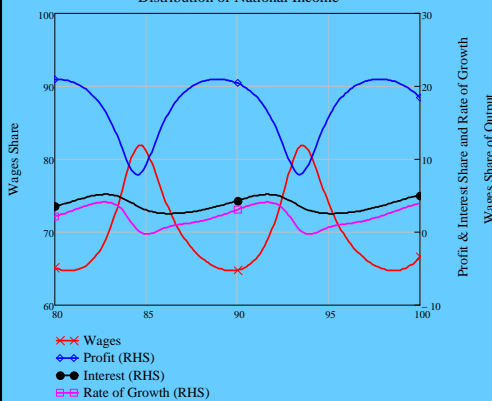
Debt and Growth Dynamics



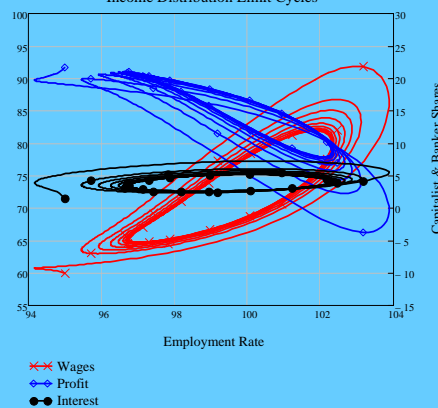
A Multi-sectoral monetary model of production

- Income distribution cycles...

Distribution of National Income

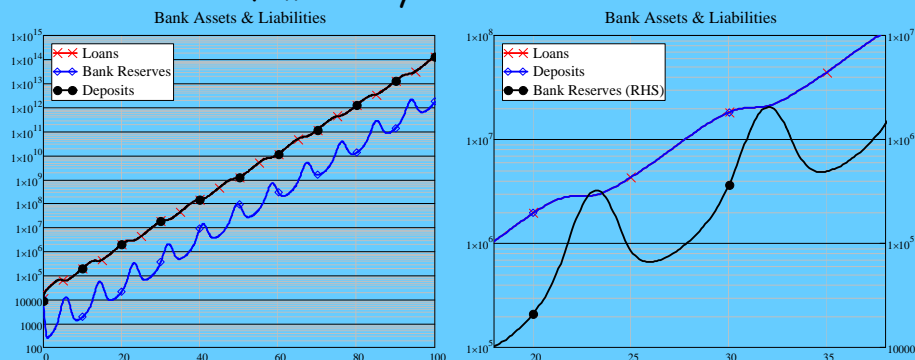


Income Distribution Limit Cycles



A Multi-sectoral monetary model of production

- Crucial role of monetary variables



- Simulation show here generates "stable instability"
 - Cycles but not breakdown
- Different parameters can generate
 - Convergence to stability; or
 - Financial collapse (Great Depression)

A Multi-sectoral monetary model of production

- Crucial characteristic that cycles are endogenous
 - General *Disequilibrium* as hallmark of a good model
- "Instability is an observed characteristic of our economy."
- For a theory to be useful as a guide to policy for the control of instability, the theory must show how instability is generated.
- The abstract model of the neoclassical synthesis cannot generate instability...
 - (Minsky, "Can "It" Happen Again? A Reprise")

Future development of model

- First "meteorological" model of capitalism
 - Causal dynamics rather than equilibrium assumptions
 - Realistic non-equilibrium multi-sectoral production
 - Designed for rising realism/complexity over time
- Parameter calibration of nonlinear, disequilibrium model
 - Two approaches to data fitting feasible
 - Fit functions and selected empirical data
 - Fit overall model and generate realistic nonlinear functions, lags, etc. from that
- Develop to generate alternative scenarios
 - *All will include cyclical, non-equilibrium future*
- Enable automatic generation of higher-dimensional multisectoral models